Unit I: Conics, Parametric Equations, and Polar Coordinates

Content Standard: Understand that a conic section is defined as the intersection of a plane and a double napped cone. Understand that a parametric equation is comprised of three variables and two linear equations. Understand how to use calculus and parametric equations to solve problems. Understand the Polar Coordinate System and how to solve problems using polar functions.

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- 2.2 Computation and Estimation
- 2.3 Measurement and Estimation
- 2.4 Mathematical Reasoning and Connections
- 2.5 Mathematical Problem Solving and Communications
- 2.7 Probability and Prediction
- 2.8 Algebra and Functions
- 2.9 Geometry
- 2.10 Trigonometry
- 2.11 Concepts of Calculus

ISTE's Educational Technology Standards *USED EVERYDAY*

- 1. Creativity and innovation
- 2. Communication and collaboration
- 3. Research and information fluency
- 4. Critical thinking, problem solving, and decision making
- 5. Digital citizenship
- 6. Technology operations and concepts

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Pacing: 8 Days

Course Content	Student Performance	Resources	Assessments
A. Conic Section	Use conic sections to find equations of parabolas,	Graphing calculator	Explorations
	ellipses and hyperbolas	Computer graphing software	Quizzes
B. Parametric Equations	Graph parametric equations, find derivatives, arc length,	AP Calculus released exams	• Exams
	and area of a surface of revolution using integration	 AP Calculus Website {www.collegeboard.com} 	Journal
C. Polar Coordinates and Polar	Use coordinate conversions	Calculus labs and student	Presentations
Graphs	to graph polar functions	 Calculus labs and student projects 	Research project
	Find slope in polar form	PowerPoint presentations	Cooperative learning
	Use integration to find area, arc length and area of	Teacher's guide	
	surface of revolution	Solution manual	
D. Kepler's Law	Use Kepler's Law to solve problems involving orbiting	APCD CD-Rom	
	of planets	Spreadsheet program	
		Geometer's sketchpad	
		United streaming	

Unit: Vectors and the Geometry of Space

Content Standard: Understand Vectors in the Plane including component form of a vector, vector operations, standard unit vector, and applications of vectors.

Understand how to find coordinates in space, dot products and cross products. Understand that cylindrical coordinates are an extension of polar coordinates.

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Pacing: 12 Days

Course Content	Student Performance	Resources	Assessments
A. Vectors in a Plane	Learn about the component form of a vector and apply	Graphing calculator	Explorations
	what they learn to physic problems	Computer graphing software	• Quizzes
B. Space Coordinates and	Find distance and vectors in	AP Calculus released exams	• Exams
Vectors in Space	space and apply them to force problems	 AP Calculus Website {www.collegeboard.com} 	Journal
	Find the dot product of,		 Presentations
C. The Dot Product	angle between, force of, and work done of two vectors	 Calculus labs and student projects 	Research project
D. The Cross Product	Apply algebraic and	PowerPoint presentations	Cooperative learning
	geometric properties of the cross product to solve force	Teacher's guide	
	problems	Solution manual	
	 Learn how to use triple scalar products 	APCD CD-Rom	
E. Lines and Planes in Space	Find equation of line in	Spreadsheet program	
	three-space	Geometer's sketchpad	
	Find distance between a point and plane, between two parallel planes, and point and a line in space	United streaming	
F. Surface in Space	Find surface equations of 3 dimensional figures		
G. Cylindrical and Spherical Coordinates	Apply knowledge about polar coordinates and adapt to cylindrical and spherical		

coordinates	
coordinates	

Unit: Vector-Valued Functions

Content Standard: A vector-valued function is a function that maps real numbers onto vectors.

State Curriculum Standard:

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- 2.5 Mathematical Problem Solving and Communications
- 2.7 Probability and Prediction
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Pacing: 12 Days

Course Content	Student Performance	Resources	Assessments
A. Vector-Valued Functions	Graph and solve problems using definition of vector- valued functions	 Graphing calculator Computer graphing software	ExplorationsQuizzes
B. Differentiation and Integration of Vector-Valued FunctionsC. Velocity and Acceleration	 Differentiate and integrate vector-valued functions Find velocity and acceleration of vector-valued functions including projectile motion 	 AP Calculus released exams AP Calculus Website {www.collegeboard.com} Calculus labs and student projects 	ExamsJournalPresentationsResearch project
D. Tangent Vectors and Normal Vectors	Find tangent and normal vectors and apply them to projectile motion	PowerPoint presentationsTeacher's guide	Cooperative learning
E. Arc Length and Curvature	Find arc length and curvature of vector-valued functions	 Solution manual APCD CD-Rom Spreadsheet program Geometer's sketchpad United streaming 	

Unit: Functions of Several Variables

Content Standard: Functions of several variable deal with two or more variables and will be in the form of f(x,y) or f(x,y,z).

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- 2.3 Measurement and Estimation
- 2.4 Mathematical Reasoning and Connections
- 2.5 Mathematical Problem Solving and Communications
- 2.7 Probability and Prediction
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Pacing: 16 Days

Course Content	Student Performance	Resources	Assessments
A. Introduction to Functions of Several Variables	 Learn what functions of several variables are about 	Graphing calculator	Explorations
	and be able to sketch their curves	Computer graphing software	• Quizzes
B. Limits & Continuity	Find the limit and continuity	AP Calculus released exams	Exams
	of functions of two and three variables	AP Calculus Website {www.collegeboard.com}	Journal
C. Partial Derivatives	Use the definition of partial	Calculus labs and student	Presentations
	derivatives to solve problems	projects	Research project
D. Differentials	Find differentials and use	PowerPoint presentations	Cooperative learning
	them to find an approximation for the value	Teacher's guide	
	of a function	Solution manual	
E. Chain Rule	Solve related rate problems using chain rule	APCD CD-Rom	
	Find partial derivative	Spreadsheet program	
	implicitly	Geometer's sketchpad	
F. Directional Derivatives and Gradients	Determine slope at point on surface by using directional derivatives and gradients	United streaming	
G. Tangent Planes and Normal Lines	Find equation of tangent plane		
H. Extrema of Functions	Find max, min, critical points, and use second partials test		

Course Content	Student Performance	Resources	Assessments
I. Applications of Extrema of Functions of Two Variables	Solve real word problems using optimization techniques and method of least squares		
J. Lagrange Multipliers	Apply constraints to optimization problems		

Unit: Multiple Integration

Content Standard: Multiple integration is taking the integral of several different variables

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Pacing: 16 Days

Course Content	Student Performance	Resources	Assessments
A. Iterated Integrals & Area in the Plane	Integrate with several variables and find the area	Graphing calculator	Explorations
	between two line using several variables	Computer graphing software	Quizzes
B. Double Integrals & Volume	Evaluate double integrals	AP Calculus released exams	Exams
	and apply them to volume problems	AP Calculus Website {www.collegeboard.com}	Journal
C. Change of Variables: Polar	Dogariba a ragion uning		 Presentations
Coordinates	Describe a region using polar coordinates and evaluate a double polar	 Calculus labs and student projects 	Research project
	integral	PowerPoint presentations	Cooperative learning
D. Center of Mass and Moments of Inertia	Find center of mass and moments of inertia of Planar	Teacher's guide	
	Laminas, Polar Coordinates	Solution manual	
E. Surface Area	Find surface area using double integrals	APCD CD-Rom	
F. Triple Integrals and	Find volume, limits, center of	Spreadsheet program	
Applications	mass and moments of inertia using triple integrals	Geometer's sketchpad	
G. Triple Integrals in Cylindrical and Spherical Coordinates	Find volume, limits, center of mass and moments of inertia using cylindrical coordinates	United streaming	
H. Change of Variables: Jacobians	Learn and apply Jacobians to change of variables for double integrals		

Unit: Vector Analysis

Content Standard: Vector analysis involves vector fields including force fields and velocity fields.

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Pacing: 16 Days

Course Content	Student Performance	Resources	Assessments
A. Vector Fields	Learn about a variety of vector fields and how to	Graphing calculator	Explorations
	sketch them	Computer graphing software	• Quizzes
B. Line Integrals	 Integrate piecewise sooth curves and find the mass of 	AP Calculus released exams	Exams
	a spring, work done by a force, and orientation of a	AP Calculus Website {www.collegeboard.com}	Journal
	curve	Oalankia laba and atudant	 Presentations
C. Conservative Vector Fields and Independence of Path	Learn the Fundamental Theorem of Line integrals	 Calculus labs and student projects 	Research project
D. Green's Theorem	Loorn/onnly Croon's	PowerPoint presentations	Cooperative learning
	 Learn/apply Green's Theorem to variety of calculus problems 	Teacher's guide	
E. Parametric Surface	Sketch and revolve	Solution manual	
	parametric surfaces to find surface area	APCD CD-Rom	
F. Surface Integrals	Evaluate surface integral	Spreadsheet program	
	and find its center of mass and orientation	Geometer's sketchpad	
G. Divergence Theorem	Learn/apply Divergence Theorem	United streaming	
H. Stoke's Theorem	Learn/apply Stoke's Theorem		

Unit: Differential Equations

Content Standard: Differential equations are equations involving the derivatives of a function or functions.

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Pacing: 10 Days

Course Content	Student Performance	Resources	Assessments
A. Exact First-Order Equations	Solve Exact Differential Equations	Graphing calculator	Explorations
B. First-Order Linear	Solve first-order linear	Computer graphing software	Quizzes
Differential Equations	equations	AP Calculus released exams	Exams
C. Second-Order Homogeneous Linear	 Learn what second-order homogenous equations are 	AP Calculus Website {www.collegeboard.com}	Journal
Equations	apply them to the real world	Calculus labs and student	Presentations
D. Second-Order Non- Homogeneous Linear	Learn what second-order non-homogenous equations	projects	Research project
Equations	are and apply them to the real world	PowerPoint presentations	Cooperative learning
E. Series Solutions of	Find solutions to power	Teacher's guide	
Differential Equations	series and Taylor series	Solution manual	
		APCD CD-Rom	
		Spreadsheet program	
		Geometer's sketchpad	
		United streaming	